

# **Labor Supply Responses and Welfare Effects from Replacing Current Tax Rules by a Flat Tax: Empirical Evidence from Italy, Norway and Sweden**

by

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## **Abstract**

This paper employs a microeconomic framework to examine the labor supply responses and the welfare effects from replacing current tax systems in Italy, Norway and Sweden by a flat tax on total income. The flat tax rates are determined so that the tax revenues are equal to the revenues as of 1992. The flat tax rates vary from 23 per cent in Italy, 25 per cent in Norway, to 29 per cent in Sweden. In all three countries the labor supply responses decline sharply with pre-reform disposable income. The results show that the efficiency costs of the current tax systems relative to a flat tax may be rather high in Norway and much lower, but positive, in Italy and Sweden. In all three countries "rich" households — defined by their pre-tax-reform income — tend to benefit more than "poor" households. In Italy and Sweden a majority will lose from a shift to a flat tax, while in Norway a majority is predicted to win.

**Key words:** Labor Supply, Taxation, Microeconomic Cross-Country Analysis.

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## 1. Introduction

During the post-war decades goods, services, labor and capital have gradually become more mobile across nations. This process of increased international mobility may have improved the allocation of resources and given substantial gains from trade and migration. To reinforce this line of development in Europe the European Union (EU) has introduced the so-called four liberties which means that goods, services, labor and capital are now allowed to move freely across the EU borders. These four liberties can now be enjoyed not only by citizens and firms within EU, but also by countries that are members of the European-Economic-Area (EEA). Increased mobility of goods, services, labor and capital creates a new climate of competition which makes it costly to maintain tax systems that differ substantially across nations. The more mobile the tax base turns out to be, the more costly it is to implement higher national tax rates than in other countries. We refer to Musgrave (1969) for an early discussion of these issues.

Labor has normally been considered to be the least mobile factor, at least when judged on the basis of European data. The dismantling of country-specific barriers may increase the mobility in European labor markets. Cultural differences and language problems may, on the other hand, have a substantial negative effect on mobility. Yet, the removal of mobility costs and the fact that (some) high skilled workers and professionals are rather mobile may in the long run prevent European nations from allowing for significant differences in the taxation of labor income. Thus, tax system competition may arise as a result of EU's introduction of the four liberties. Since progressive tax systems normally tax the higher income of skilled workers and professionals more heavily than the lower income of the lesser skilled, tax system competition will most likely move the tax systems towards a proportional (European) tax structure; see Sinn (1997) for a theoretical discussion where the tax competition equilibrium implies zero tax rates. However, by relaxing the extreme zero mobility costs assumption of Sinn (1997), a tax competition equilibrium with a positive proportional tax rate may be a more likely outcome.

Capital is conventionally considered to be a mobile factor, and the introduction of EU's four liberties has removed the last barriers against free capital movements throughout Western Europe. This fact has made the taxation of capital and firm income more equal across European countries and the trend is towards a common proportional tax rate. For example, both Norway and Sweden implemented tax reforms in the early 1990s where the main objective

was to relax taxation of capital income by introducing a flat tax rate on capital income.<sup>4</sup> The mobility-induced proportional capital and firm income taxation may change the progressive taxation of labor income towards a proportional tax system, and for three reasons. First, progressive labor income taxes may be perceived unfair by a voting majority of wage earners when people with capital income face proportional taxes. Second, if capital and firm income are taxed differently from labor income, this may give incentives to black market and/or tax evasion activities. To handle these types of economic crime problems government authorities may find it appropriate to change taxation of labor income towards the proportional tax on other types of income. Finally, as suggested by Gordon and Nielsen (1997), when labor income is taxed at a progressive rate but firm income is taxed at an uniform (proportional) rate, the progressive labor income tax may cause an efficiency cost.

The Scandinavian countries have gradually developed the welfare state institutions during this century. An important element in this development was the construction of institutions for redistributing income through progressive taxation, social benefits and transfers, wage policy, public education and public health care. The economic implications of these welfare state institutions have been questioned recently, primarily due to substantial efficiency losses, see Rosen (1996). In particular, it has been pointed to the negative impact on overall economic efficiency from having progressive income taxes. Apart from anecdotal evidences and studies based on aggregated data there are, however, few empirical welfare analyses that take into account the heterogeneity among households and firms and thus the impact on the distribution of individual welfare of changes in the tax and benefit structure, see e.g. Atkinson (1995).

In this paper we have employed a labor supply model - estimated on data from three countries - to simulate labor supply responses of married couples from replacing the tax systems as of 1992 by a flat tax on total income. The focus on married couples is motivated by the fact that married females are considered to be more responsive to changes in tax rates than other individuals. The mean level and distribution of the labor supply responses depend on preferences, demographic and educational structure, tax and benefit rules, and other institutional constraints. Although the estimates of some of the key parameteres are quite equal across the three countries, other parameters as well as tax systems and other aspects of the choice environment differ. From a methodological point of view it is of interest to study whether country-specific variations in preferences and budget constraints create significant

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<sup>4</sup> The post-reform flat tax rates on capital income were 28% and 30% in Norway and Sweden, respectively.

differences in the labor supply responses when the households are exposed to similar changes in tax rules.

The paper is organized as follows. Section 2 gives a brief, but self-contained, description of our policy evaluation methodology which is based on a particular framework of modelling labor supply, see Dagsvik (1994) and Aaberge, Colombino and Strøm (1998) for further details. The empirical specifications of the model and the estimation results, based on Italian, Norwegian and Swedish tax return data for married couples, are given in Appendix 1. Section 3 reports the policy simulation results, and Section 4 summarizes our findings.

## **2. Methodological framework**

Our policy evaluation methodology relies on a microeconomic labor supply model. Labor supply behavior is analysed as a discrete choice problem, where the choice-alternatives are "job-packages". These job-packages are characterized by specific attributes such as wage rates, hours of work and other non-pecuniary variables. In addition, this framework is able to take into account that there are quantity constraints in the market, in the sense that different types of jobs are not equally available to every agent. Agents differ by qualifications, and jobs differ with respect to qualifications required.

Labor supply models are helpful devices for examining individual welfare effects from tax reforms. Normally, the welfare effects are measured by various Hicks-compensating measures, see Auerbach (1985), Hausman (1981) and King (1987) for a discussion of alternative money metrics of welfare change, and Hammond (1990) for arguments in favor of using Equivalent Variation (EV). Loosely speaking, EV is measured as the amount of money that has to be added to/subtracted from the household's disposable income under the initial tax rules in order to make the household indifferent between the initial and the alternative tax system. Note that EV is measured at the household level. EV sums up the household's net welfare gain/loss associated with behavioral responses induced by tax reforms, say, increased consumption and reduced leisure.

An empirical micro-model — such as the one we apply here — is designed to account for observed as well as unobserved heterogeneity. Unobserved heterogeneity arises from the fact that as econometricians we are unable to observe all factors that affect individual tastes and opportunities. These unobservables are modelled as random variables, which imply that a money metric of welfare change, at the household level, such as EV, becomes a random variable; see King (1987) and Atkinson (1990). In other words, micro-econometric models allow for studying the distribution of EV. The mean of this distribution is the overall mean of the welfare gain or loss which indeed can be interpreted as being derived from an utilitarian

social welfare function. Note that most empirical analyses of tax reforms solely report the mean EV, see e.g. Hausman (1985), Hausman and Poterba (1987) and Blomquist (1983), despite the fact that microeconomic models with heterogeneous agents are estimated. Heterogeneous preferences and opportunity sets are important not only for estimation, but also for welfare analysis. Our approach allows for an evaluation that identifies both losers and winners.

### 2.1. The Simulation Framework

We will first give a brief outline of the microeconomic model. For expository reasons we focus on an one-person household. Next we will explain how the simulations have been performed.

Each agent is assumed to face a set of non-market and market opportunities. These sets may vary across households. A market opportunity is characterized by hours  $h$ , a wage rate  $w$  and other characteristics beyond hours and wages, say commuting time and the working environment. We let  $j$  summarize these other characteristics. A non-market opportunity carries zero hours and zero wage rates, but also in this case there may be many different opportunities according to different leisure and home production activities. Let  $U_i(C, h, j)$  denote the utility for agent  $i$  of consumption  $C$ , hours  $h$  (or, equivalently, leisure, with a positive marginal utility of leisure) and other job-characteristics  $j$ . The argument  $j$  in the utility function accounts for the fact that the agent's preferences may vary across job characteristics beyond hours of work and the wage rate.

The economic budget constraint is given by

$$C = f(wh, I), \quad (1)$$

where  $I$  is non-labor income and  $f$  is a function that transforms gross income into after-tax income. To this end we suppress the fact that the  $f$ -function should have a subscript  $i$  to indicate that tax deductions vary across households. The price index of the composite good (called consumption) is equal to one. When inserting the budget constraint into the utility function we get  $U_i(f(wh, I), h, j)$ . We will assume that

$$U_i(f(wh, I), h, j) = v_i(f(wh, I), h) \varepsilon_i(h, w, j) \quad (2)$$

where  $v(C, h)$  is a positive, deterministic function which is quasi-concave in  $(C, h)$ , increasing in the first argument and decreasing in the second. The term  $\varepsilon_i(h, w, j)$  is a random taste-shifter that is supposed to capture the effect of unobservable attributes associated with opportunity  $j$ . Note that this term is viewed as random from the econometrician's point of view,

while it is assumed known to the agent. Specifically  $\varepsilon_i(h, w, j)$  accounts for the fact that for a given agent, tastes may vary over opportunities, hours and wages, and for a given opportunity, tastes may vary across agents. Let  $B_i(h, w)$  denote the set of market opportunities with hours  $h$  and wage rate  $w$  that are feasible to agent  $i$ , whilst  $B_i(0,0)$  is the set of non-market opportunities. The set  $B_i$  contains opportunities with fixed hours and wages, and where the remaining characteristics, captured by  $j$ , vary. Thus,  $j \in B_i(h, w)$ ,  $h \geq 0$ ,  $w \geq 0$ . Again, we may assume that the sets  $B_i$  are known to the agents, but unknown to the econometricians. Finally, define

$$V_i(h, w) = \max_{j \in B_i(h, w)} U_i(f(wh, I), h, j). \quad (3)$$

For agent  $i$ ,  $V_i(h, w)$  is the utility of the most preferred opportunity among the feasible opportunities with hours  $h$  and wage rate  $w$  and can be considered as the conditional indirect utility function, given hours of work and the wage rate.

From (2) and (3) we get

$$V_i(h, w) = \mathbf{y}_i(h, w) e_i(h, w) \quad (4)$$

where

$$e_i(h, w) = \max_{j \in B_i(h, w)} \mathbf{e}_i(h, w, j) \quad (5)$$

and

$$\mathbf{y}_i(h, w) = v_i(f(wh, I), h). \quad (6)$$

Recall that hours and wage rates are fixed for each job so that when a job has been chosen, then hours and wage rate follow. The individual agent is assumed to choose the job from his/her opportunity set that maximizes utility. The corresponding hours and wage rate,  $(h, w)$ , therefore follow from maximizing  $V_i(h, w)$ .

In order to obtain an explicit expression for the structure of the choice probabilities of realized hours and wage rates we have to make further assumptions about the distribution of the random components in this model. When the the taste-shifters are i.i.d. with distribution

$$P(\mathbf{e}_i(h, w, j) \leq y) = \exp\left(-\frac{1}{y}\right) \quad y > 0, \quad (7)$$

Dagsvik (1994) has demonstrated that the choice probabilities attain a multinomial logit form. To deal with the problem of unobserved opportunity sets we specify densities that reflect the distribution of the opportunities. The parameters of these densities may depend on observed characteristics.

Let  $\mathbf{j}(h, w)$  be the probability that agent  $i$  shall choose a job with hours and wage rate  $(h, w)$ , i.e.

$$\mathbf{j}_i(h, w) \equiv P\left[V_i(h, w) = \max_{x,y} V_i(x, y)\right] = \frac{\mathbf{y}_i(h, w) g_{i0} g_i(h, w)}{\mathbf{y}_i(0,0) + g_{i0} \int_{x>0} \int_{y>0} \mathbf{y}_i(x, y) g_i(x, y) dx dy} \quad (8)$$

for  $h > 0, w > 0$ .

The probability of not working equals

$$\mathbf{j}_i(0,0) = \frac{\mathbf{y}_i(0,0) g_{i0}}{\mathbf{y}_i(0,0) + g_{i0} \int_{x>0} \int_{y>0} \mathbf{y}_i(x, y) g_i(x, y) dx dy} \quad (9)$$

The density function  $g_i(h, w)$  can be interpreted as the mean of the fraction of feasible jobs with hours  $h$  and wage rate  $w$ . This density function arises from the fact that in the opportunity sets there are unobservable (to the econometrician) attributes associated with feasible jobs with hours  $h$  and wage rate  $w$ . Similarly,  $g_{i0}$  is the mean of the fraction of opportunities that are feasible job-opportunities. Note that the opportunity density,  $g_i(\cdot, \cdot)$  may depend on the production technology of the firms as well as of the wage setting policies of the firms and the unions.

The functional form of (8) and (9) is particularly attractive. The labor supply density  $\mathbf{j}(h, w)$  is expressed as a simple function of the structural term of the utility function,  $\psi(\cdot)$ , and of  $g_0 g(\cdot)$ , which is an aggregate representation of the set of feasible job opportunities. The extension of the model to deal with the joint decisions of husband and wife is analogous to the case of single person households. Then the household is assumed to have preferences over household consumption and leisure for the husband and wife. For further details about the microeconomic model we refer to Aaberge et al. (1998).

The model has been estimated on Swedish (1981), Norwegian (1986) and Italian data (1987). In all three datasets the population is restricted to married couples. Households with an income from self-employment that exceeds 20% of total gross income are excluded from the samples. For the included households, income from self-employment and capital-income have

been added to net household income and are treated as exogenous. We have restricted the ages of the husband and the wife to be between 20 and 68 years old. The sample sizes vary from 1640 in Sweden to 2960 in Italy. The Swedish data set does not allow us to estimate participation probabilities. However, the Swedish participation rates in 1981 were very high, even for females, and we might have gained little from including participation/non-participation observations in estimating the model. Empirical specifications and estimation results are reported in Appendix 1.

The estimated models are used to simulate the labor supply, incomes and tax revenue that follow from imposing the 1992 tax systems in all three countries. For Norway we have used the population characteristics of 1992 in the simulation experiment, whilst for the two other countries we have employed the characteristics used in estimating the model. For all three countries we have used all details of the tax system as of 1992 to simulate labor supply, incomes and tax revenue in 1992. Next, we have run the model to simulate the behavioral and welfare effects of replacing the 1992 system by a flat tax on total income. Note that these simulation experiments are stochastic because the choice opportunities and the preferences are random from the econometrician's point of view. Furthermore, it should be emphasized that the results reported below depend on the population characteristics and consequently, these result may change when these characteristics change.

The stochastic simulations are done in the following way. First, for each household we draw wage rates (male and female) from the wage distribution for the household. Throughout the experiments we keep this wage rates fixed. Second, for each household  $i$  we draw  $r$  points:  $(h_{Mi}(t), h_{Fi}(t), \varepsilon_i(t)); t=1,2,\dots,r$ ; where the subscripts attached to hours indicate male and female. Offered hours that are feasible for each household are drawn from a uniform distribution with full-time and part-time peaks, while  $\varepsilon_i(t)$  are drawn from the distribution given in (7). The optimal pair of jobs for each married couple is then derived from maximizing the utility function, given in (2), with respect to  $t$ ; that is the jobs that yield the highest utility for the household are chosen.

Welfare gains and losses are measured by Equivalent Variation (EV). To describe the method of calculation it appears convenient to introduce the following notation. Let

$$\tilde{V}_i(EV, f) \equiv \max_{h,w} \max_{j \in B_i(h,w)} \left( U_i(EV + f(hw, I), h, j) \right). \quad (10)$$

Note that  $\tilde{V}_i(EV, f)$  is the indirect utility for agent  $i$  under tax regime  $f$ , when the agent is endowed with non-taxable non-labor income  $EV$ .

We define equivalent variations for the agent as the amount  $EV$  determined by



$$\tilde{V}_i(EV, f_0) = \tilde{V}_i(0, f_1) \quad (11)$$

where the subscript 0 denotes the initial (reference) tax regime, and subscript 1 the alternative tax regime. Since the utility function is random so is also EV. The parameters of the distribution of EV are assessed by means of stochastic simulations.

### 3. Results of simulations

#### 3.1 Labor Supply Elasticities

For each country the labor supply elasticities are derived by predicting labor supply (by stochastic simulation) for each household (wife and husband) when the tax rates are increased by 1 per cent. Individual responses are averaged across households to yield aggregate labor supply elasticities. Note that the elasticities depend on preferences, demographic and educational structure, tax functions and other constraints prevailing in the years that the elasticities refer to. These years are the years of the datasets used in estimating the model; for Italy it is 1987, for Norway 1986 and for Sweden 1981. Aggregated uncompensated elasticities are reported in Tables 1-3. The "estimates" of the elasticities are based on 10 sets of simulation. In Tables 1-3 we report the mean and standard deviations for each elasticity.

**Table 1. Uncompensated aggregate labor supply elasticities, Italy 1987.\***

| Type of elasticity  | Male elasticities |                   | Female elasticities |                   |
|---|-------------------|-------------------|---------------------|-------------------|
|   | Own wage          | Cross wage        | Own wage            | Cross wage        |
| Elasticity of the probability of participation              | 0.046<br>(0.001)  | -0.081<br>(0.002) | 0.654<br>(0.006)    | -0.357<br>(0.008) |
| Elasticity of the conditional expectation of hours supply   | 0.007<br>(0.001)  | -0.035<br>(0.002) | 0.078<br>(0.003)    | -0.136<br>(0.002) |
| Elasticity of the unconditional expectation of hours supply | 0.053<br>(0.002)  | -0.116<br>(0.002) | 0.737<br>(0.006)    | -0.489<br>(0.008) |

\*Standard deviations in parentheses

**Table 2. Uncompensated aggregate labor supply elasticities, Norway 1986.\***

| Type of elasticity  | Male elasticities |                  | Female elasticities |                  |
|---|-------------------|------------------|---------------------|------------------|
|   | Own wage          | Cross wage       | Own wage            | Cross wage       |
| Elasticity of the probability of participation              | 0.17<br>(0.004)   | -0.03<br>(0.004) | 0.37<br>(0.009)     | -0.12<br>(0.008) |
| Elasticity of the conditional expectation of hours supply   | 0.11<br>(0.002)   | -0.05<br>(0.004) | 0.54<br>(0.007)     | -0.12<br>(0.008) |
| Elasticity of the unconditional expectation of hours supply | 0.28<br>(0.005)   | -0.08<br>(0.005) | 0.91<br>(0.11)      | -0.24<br>(0.014) |

\*Standard deviations in parentheses

**Table 3. Uncompensated aggregate labor supply elasticities, Sweden 1981.\***

| Type of elasticity  | Male elasticities |                   | Female elasticities |                   |
|---|-------------------|-------------------|---------------------|-------------------|
|   | Own wage          | Cross wage        | Own wage            | Cross wage        |
| Elasticity of the conditional expectation of hours supply | -0.020<br>(0.001) | -0.021<br>(0.002) | 0.070<br>(0.006)    | -0.065<br>(0.008) |

\*Standard deviations in parentheses

Tables 1-3 indicate that in all three countries female labor supply is more responsive than male labor supply. Moreover, the cross wage elasticities are all negative and sizeable relative to the own wage elasticities. This latter result is important to keep in mind when microeconomic results- as those reported here – are compared with labor supply elasticity estimates based on aggregate time series. The latter often tend to be lower than microeconomic based estimates of the own wage elasticities. However, the results reported here suggest that the time series estimates based on aggregate data might be downward biased when considered as estimates of the own wage elasticities. Wage rates for males and females typically vary in a similar way over the business cycle. Although estimation based on aggregate time series data often are done separately for males and females, very few time series analysts account for the fact that most

adults live together in marriage or cohabitation. Consequently, they estimate the impact on labor supply of a simultaneous change in male and female wage rates over time, and where the own-wage effects are not disentangled from the cross effects. Therefore, time series analysts tend to pick up the net effect defined as the own wage rate elasticity minus the cross wage elasticity. Also in our microeconomic model we get low net effects. For instance in the case of Italy we observe that the net effect on labor supply, given participation, is numerically small and negative both for men and women. The last row of Table 1 gives the labor supply elasticities in the total population and we observe that the net effect of an overall wage increase across gender dampens the labor supply response quite drastically compared to the impact given by the own wage elasticities. From Tables 1-3 we observe that this pattern is the same across countries.

Despite the differences in the choice environments and to some minor extent the differences in preferences across the three countries, the labor supply elasticities are quite similar. The labor supply elasticities suggest that the working females in Italy and Sweden are less responsive than in Norway. Since the late 1960s the female participation rate in Sweden has been the highest in the world. Thus, for the last two-three decades the labor market attachments of Swedish women have been very much the same as for men in Sweden. In addition Sweden is a highly unionized country with strict regulations of working hours. From Table 3 we see that the labor supply elasticities both for Swedish men and women are numerically small. We note that the mean labor supply curve for Swedish men even tend to be backward bending. The weak labor supply responses, given participation, in Italy may be due to relative high rigidity of working hours. This rigidity implies – like in Sweden - a more stringent choice for Italian workers: Either a normal "9 to 5" working day or not working at all; for further details about rigidity of working hours in Italy, see Di Tommaso(1998) and Malerba (1995).

The high rigidity of working hours in Italy and Sweden is well documented in OECD statistics. According to OECD (1997), the ratios of part time jobs to full time jobs in Sweden and Italy in 1996 were among the lowest in OECD-Europe (23.5 % and 20.9%, respectively). By contrast, the part-time ratio in Norway was 46.5% which was the second highest in OECD Europe. Thus, the Norwegian labor market is rather flexible by European standards<sup>5</sup>. These differences across countries in the rigidity of offered working hours are indeed reflected in the

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<sup>5</sup> As an example, in Statistics Norway, which employs around 800 people, mostly women, there are above 60 different contracts of working hours.

estimates of  $g_0$  reported in Appendix 1. Rigidity of working hours may explain why labor supply elasticities are low.

Tables 1 and 2 demonstrate that the participation decision in Italy is more responsive to changes in the economic incentives to work than in Norway. Given the differences in rigidity of working hours alluded to above, this result may appear to be counterintuitive. However, because the participation rate among married females in Italy is rather low by Scandinavian standards, there is a larger potential for increased participation in Italy than in the Scandinavian countries. The lower the participation rate is, the higher is the percentage increase in participation when working incentives are improved.

In Tables 4-6 we illustrate the variation of the labor supply elasticities with household income. A striking similarity across the three countries is the decline of the labor supply elasticities with income. For the richest household the labor supply elasticities for both gender are close to zero, and they are even negative for males in Sweden and Italy but also for females in Sweden. Thus, for the poorest household the labor supply curve is upward sloping, while for the richest it tends to be backward bending.<sup>6</sup>

**Table 4. Income-dependent uncompensated aggregate elasticities, Italy 1987**

| Type of elasticity  | Deciles in the disposable income distribution | Male elasticities |            | Female elasticities |            |
|---|---|-------------------|------------|---------------------|------------|
|   |   | Own wage          | Cross wage | Own wage            | Cross wage |
| Elasticity of the probability of participation              | 10 percent poorest                            |                   |            |                     |            |
|   | 80 percent in the middle                      | 0.053             | -0.109     | 2.837               | -1.089     |
|   | 10 percent richest                            | 0.051             | -0.086     | 0.742               | -0.356     |
| Elasticity of the conditional expectation of hours supply   | 10 percent poorest                            |                   |            |                     |            |
|   | 80 percent in the middle                      | 0.021             | -0.017     | 0.467               | -1.410     |
|   | 10 percent richest                            | 0.011             | -0.045     | 0.100               | -0.150     |
| Elasticity of the unconditional expectation of hours supply | 10 percent poorest                            |                   |            |                     |            |
|   | 80 percent in the middle                      | 0.075             | -0.126     | 3.441               | -1.454     |
|   | 10 percent richest                            | 0.062             | -0.130     | 0.832               | -0.501     |

<sup>6</sup> The compensated elasticities exhibit a similar variation with income; see Aaaberger et al (1990,1993,1995,1998).

|  |  |        |        |       |        |
|--|--|--------|--------|-------|--------|
|  |  | -0.041 | -0.029 | 0.035 | -0.181 |
|--|--|--------|--------|-------|--------|

**Table 5. Income dependent aggregate labor supply elasticities, Norway 1986.**

| Type of elasticity  | Deciles in the distribution of disposable income | Male elasticities |            | Female elasticities |            |
|---|--|-------------------|------------|---------------------|------------|
|   |  | Own wage          | Cross wage | Own wage            | Cross wage |
| Elasticity of the probability of participation              | 10 percent poorest                               | 1.89              | -1.04      | 1.85                | -1.44      |
|   | 80 percent in the middle                         | 0.09              | -0.08      | 0.66                | -0.29      |
|   | 10 percent richest                               | 0.03              | 0.00       | 0.07                | -0.03      |
| Elasticity of the conditional expectation of hours supply   | 10 percent poorest                               | 0.29              | -0.15      | 1.04                | -1.04      |
|   | 80 percent in the middle                         | 0.07              | -0.09      | 0.78                | -0.29      |
|   | 10 percent richest                               | 0.03              | -0.01      | 0.12                | -0.06      |
| Elasticity of the unconditional expectation of hours supply | 10 percent poorest                               | 2.23              | -1.18      | 3.09                | -2.23      |
|   | 80 percent in the middle                         | 0.16              | -0.17      | 1.49                | -0.57      |
|   | 10 percent richest                               | 0.06              | -0.01      | 0.19                | -0.08      |

**Table 6. Income-dependent aggregate uncompensated labor supply elasticities, Sweden 1981.**

| Type of elasticity  | Deciles in the distribution of disposable income | Male elasticities |            | Female elasticities |            |
|---|--|-------------------|------------|---------------------|------------|
|   |  | Own wage          | Cross wage | Own wage            | Cross wage |
| Elasticity of the conditional expectation of hours supply | 10 percent poorest                               | 0.054             | -0.038     | 0.069               | -0.031     |
|   | 80 percent in the middle                         | -0.025            | -0.019     | 0.034               | -0.067     |
|   | 10 percent richest                               | -0.047            | -0.024     | -0.037              | -0.072     |

### 3.2 Tax reform simulations

The married couple version of the model outlined in Section 2 is employed to simulate labor supply responses and individual welfare effects from introducing a flat tax on income. The tax reform simulations are performed in a partial equilibrium setting, as in Browning (1987). In our framework, this means that the opportunity densities of offered wages and hours are considered as exogenously given and they are thus unaffected by a change of tax systems. Moreover, the total number of jobs are assumed to increase (decrease) with increasing (decreasing) labor supply.

As mentioned above, for all three countries the estimated microeconomic models are applied to simulate labor supply, incomes and tax revenue in 1992. This year was chosen because similar tax reforms were introduced in Norway 1992, Sweden 1990 and in Italy gradually over years in the late 1980s and early 1990s. The tax revenue is kept fixed at the 1992 level when the model is used to assess the impacts of introducing a flat tax on income.

The results of Tables 7-9 show that the labor supply responses from replacing the 1992-tax-regime ("current tax regime") by a proportional tax are rather strong in Norway, in particular for females. The labor supply responses decrease with increasing pre-reform household income, which is in line with the predictions of the income-dependent elasticities. It should also be noted that for Norway and Sweden a shift to a flat tax implies that the "poor" households experience reduced marginal tax rates and increased average tax rate. Thus, the substitution as well as the income effect predict higher labor supply. For the "rich" households both the marginal and the average tax rates decrease. Consequently, the substitution and income effects for "rich" households have different signs and thus have counteracting impacts on labor supply. In Italy the lowest marginal tax rate under the 1992 tax regime is below the proportional tax rate calculated here.

In the model employed in this paper not every working hour is equally likely to be available in the opportunity set. Opportunities with full-time working loads are more likely to be available in the choice sets. After a change to proportional taxation the market opportunities with long working hours carry lower marginal tax rates than under the 1992 regime. Thus participation may become more attractive and hours worked makes a discrete jump from zero to rather long hours. Note that a traditional – text book - labor supply model would not be able to capture this discrete jump in labor supply.

As an implication of these labor supply responses gross as well as net income increase for almost all households in all three countries. The increase in income for the "poorest"

households in Norway is rather strong and follows from the strong labor supply responses.

Note that the total tax revenues are kept constant at the 1992 national levels.

Table 10 reports the Gini coefficients of gross and disposable household income. The results for Norway demonstrate that even inequality in the distribution of disposable income decreases substantially, which mainly is due to the strong labor supply responses among "poor" households. By contrast, for Sweden we find that the inequality in the distribution of disposable income increases. For Italy we find only minor changes in income inequality.

**Table 7. Participation rates, annual hours of work, gross income, disposable income and taxes for married couples under alternative tax regimes by disposable household income in 1992. Italy**

|                                     |     | Participation Rates per cent |      | Annual hours of work |      |                         |      | Households, 1000 ITL 1992 |                     |                    |
|-------------------------------------|-----|------------------------------|------|----------------------|------|-------------------------|------|---------------------------|---------------------|--------------------|
|                                     |     |                              |      | Given Participation  |      | In the total population |      | Gross Income              | Taxes <sup>1)</sup> | Dis-posable income |
|                                     |     |                              |      | F                    | M    | F                       | M    |                           |                     |                    |
| 1992-<br>tax rules                  | I   | 4.3                          | 97.0 | 1529                 | 1832 | 66                      | 1777 | 19756                     | 3656                | 16100              |
|                                     | II  | 38.5                         | 96.3 | 1691                 | 2036 | 651                     | 1961 | 44877                     | 10845               | 34032              |
|                                     | III | 70.0                         | 94.4 | 1809                 | 2053 | 1265                    | 1939 | 90452                     | 21047               | 69405              |
|                                     | IV  | 38.2                         | 96.2 | 1711                 | 2017 | 654                     | 1940 | 46920                     | 11146               | 35774              |
| Proportional<br>taxes <sup>1)</sup> | I   | 4.3                          | 97.5 | 1398                 | 1855 | 62                      | 1809 | 20394                     | 4882                | 15512              |
|                                     | II  | 36.5                         | 96.2 | 1712                 | 2058 | 625                     | 1981 | 45717                     | 10931               | 34786              |
|                                     | III | 67.4                         | 94.6 | 1819                 | 2091 | 1225                    | 1979 | 91544                     | 19132               | 72411              |
|                                     | IV  | 36.4                         | 96.2 | 1729                 | 2041 | 692                     | 1963 | 47765                     | 11146               | 36619              |

1) The proportional tax rate of 23.3 per cent is determined by model simulation when the tax revenue is held fixed equal to the 1992 tax revenue.

Note that

- I = 10 per cent poorest households
- II = 80 per cent in the middle of the income distribution
- III = 10 per cent richest households
- IV = all households

**Table 8. Participation rates, annual hours of work, gross income, disposable income and taxes for married couples under alternative tax regimes by disposable household income in 1992. Norway**

|                                     |     | Participation Rates per cent |      | Annual hours of work |      |                         |      | Households, NOK 1992 |                     |                    |
|-------------------------------------|-----|------------------------------|------|----------------------|------|-------------------------|------|----------------------|---------------------|--------------------|
|                                     |     |                              |      | Given Participation  |      | In the total population |      | Gross Income         | Taxes <sup>1)</sup> | Dis-posable income |
|                                     |     |                              |      | F                    | M    | F                       | M    |                      |                     |                    |
| 1992-<br>tax rules                  | I   | 41.5                         | 74.1 | 926                  | 1833 | 386                     | 1360 | 160158               | 36454               | 123705             |
|                                     | II  | 77.3                         | 98.4 | 1494                 | 2432 | 1154                    | 2394 | 372208               | 115816              | 256392             |
|                                     | III | 96.4                         | 99.9 | 2279                 | 2846 | 2198                    | 2846 | 650958               | 235295              | 415662             |
|                                     | IV  | 75.4                         | 96.0 | 1562                 | 2427 | 1178                    | 2331 | 383495               | 119437              | 264058             |
| Proportional<br>taxes <sup>1)</sup> | I   | 73.2                         | 96.2 | 1756                 | 2660 | 1286                    | 2557 | 413326               | 102137              | 311189             |
|                                     | II  | 80.6                         | 99.5 | 1761                 | 2743 | 1419                    | 2729 | 471282               | 116107              | 355175             |
|                                     | III | 95.8                         | 99.9 | 2311                 | 2906 | 2213                    | 2902 | 672104               | 163658              | 508446             |
|                                     | IV  | 81.4                         | 99.2 | 1825                 | 2751 | 1485                    | 2730 | 485481               | 119445              | 366036             |

1) The proportional tax rate of 25.4 per cent is determined by model simulation when the tax revenue is held fixed equal to the 1992 tax revenue.

Note that  
 I = 10 per cent poorest households  
 II = 80 per cent in the middle of the incomedistribution  
 III = 10 per cent richest households  
 IV = all households

**Table 9. Annual hours of work, gross income, disposable income and taxes for married couples under alternative tax regimes. Sweden**

|                                     |     | Annual hours of work,<br>Given participation |       | Households, SEK 1992 |                     |                      |
|-------------------------------------|-----|--|-------|----------------------|---------------------|----------------------|
|                                     |     | F  | M     | Gross<br>income      | Taxes <sup>1)</sup> | Disposable<br>income |
| 1992-<br>tax rules                  | I   | 1 147  | 1 903 | 221 966              | 55 757              | 166 209              |
|                                     | II  | 1 690  | 2 117 | 382 603              | 110 792             | 271 811              |
|                                     | III | 1 847  | 2 339 | 706 351              | 245 257             | 461 094              |
|                                     | IV  | 1 656  | 2 126 | 401 227              | 119 838             | 281 389              |
| Proportional<br>Taxes <sup>1)</sup> | I   | 1 188  | 1 977 | 232 468              | 67 835              | 164 632              |
|                                     | II  | 1 721  | 2 209 | 399 407              | 115 211             | 284 195              |
|                                     | III | 1 874  | 2 464 | 741 690              | 208 837             | 532 853              |
|                                     | IV  | 1 683  | 2 211 | 416 952              | 119 839             | 297 113              |

1) The proportional tax rate of 29.5 per cent is determined by model simulation when the tax revenue is held fixed equal to the 1992 tax revenue.

Note that  
 I = 10 per cent poorest households  
 II = 80 per cent in the middle of the incomedistribution  
 III = 10 per cent richest households  
 IV = all households

**Table 10. Gini coefficients of distributions of gross and disposable income for couples in Italy, Norway and Sweden**

| Tax system            | Nation | Gross income | Disposable<br>income |
|-----------------------|--------|--------------|----------------------|
| 1992 tax rules        | Italy  | .243         | .234                 |
|                       | Norway | .205         | .177                 |
|                       | Sweden | .192         | .164                 |
| Proportional taxation | Italy  | .238         | .238                 |
|                       | Norway | .165         | .165                 |
|                       | Sweden | .202         | .202                 |

Tables 11-13 give information on the distribution of equivalent variation by household income.. Due to the responsive female labor supply in Norway nearly all (99%) win from replacing the 1992 tax system by a flat tax. Only a few poor households lose. In the first decile of the pre-reform income distribution 8.6 per cent is predicted to lose from having a flat tax rather than the progressive tax structure of 1992. In Italy and Sweden the proportions of losers are rather



high, in fact, in these two countries a majority is predicted to lose from replacing the 1992 tax rules by a flat tax (59 and 56%, respectively). In Norway and Sweden, and to some minor extent in Italy, the proportion of winners increases with rising pre-reform household income. Note that the only measure of welfare change one is allowed to report in an ordinalist framework is the fractions of losers and winners in the population

However, if one allows for an interpersonal comparisons of utility differences based on a money measure of welfare say, EV, one can compare the magnitudes of EV given in Tables 11-13. The mean EV in all three countries is positive which suggests that there are efficiency costs related to the 1992 tax regimes compared to proportional taxation. Tables 11-13 report the mean EV relative to the tax revenue and the results indicate that the costs of the 1992 tax system relative to a flat tax vary from 1.5 per cent for Italy, 4.8 per cent for Sweden, to as much as 34.2 per cent for Norway.

King (1987) argues that a small mean welfare gain may shadow for a large variation in gains and losses across households. Thus, King stresses the importance of accounting for heterogeneity when making welfare assessments of tax reforms. Hammond (1990) puts forward the same warnings. Our results confirm the relevance of these warnings. Although only one per cent of the population lose from the considered tax reform in Norway, between 56 and 59 per cent lose in Italy and Sweden. In Italy the mean welfare loss among the losers is ITL 1 029 000, while the mean gain among the winners is ITL 1 890 000. In Sweden the mean loss among the losers is SEK 8 252, while the mean gain among the winners is approximately three times higher.

**Table 11. Distribution of equivalent variation by household income<sup>1)</sup> under 1992-taxes.**

**Italy**

| Equivalent variations, 1000 ITL 1992 |       |                                     |                        |       |                                     |                        |      |                                     |
|--------------------------------------|-------|-------------------------------------|------------------------|-------|-------------------------------------|------------------------|------|-------------------------------------|
|                                      | Total |                                     | Losers                 |       |                                     | Winners                |      |                                     |
|                                      | Mean  | EV relative to average tax Per cent | Per cent of population | Mean  | EV Relative to Average tax Per cent | Per cent of population | Mean | EV relative to average tax Per cent |
| I                                    | 165   | 4.5                                 | 58.5                   | -1032 | -28.0                               | 41.5                   | 1860 | 51.8                                |
| II                                   | 120   | 1.1                                 | 60.1                   | -1030 | -9.6                                | 39.9                   | 1855 | 16.7                                |
| III                                  | 517   | 2.5                                 | 51.8                   | -1008 | -4.8                                | 48.2                   | 2157 | 10.3                                |
| IV                                   | 164   | 1.5                                 | 59.1                   | -1029 | -9.4                                | 40.9                   | 1890 | 16.5                                |

- 1) Note that I = 10 per cent poorest households  
 II = 80 per cent in the middle of the distribution of households' disposable income  
 III = 10 per cent richest households  
 IV = all households

**Table 12. Distribution of equivalent variation by household income<sup>1)</sup> under 1992-taxes.**

**Norway**

| Equivalent variations, NOK 1992 |  |                                |        |  |                                |         |  |      |
|---------------------------------|--|--------------------------------|--------|--|--------------------------------|---------|--|------|
| Total                           |  |                                | Losers |  |                                | Winners |  |      |
| Mean                            | EV<br>relative to<br>average tax<br>Per cent | Per cent<br>of popu-<br>lation | Mean   | EV<br>Relative to<br>Average tax<br>Per cent | Per cent<br>of popu-<br>lation | Mean    | EV<br>relative to<br>average tax<br>Per cent |      |
| I                               | 21799  | 59.8                           | 8.6    | -3694  | -11.8                          | 91.4    | 24132  | 65.1 |
| II                              | 38199  | 33.0                           | 0.3    | -1301  | -2.2                           | 99.7    | 38288  | 33.0 |
| III                             | 80811  | 34.3                           | 0.0    | -  | -                              | 100.0   | 80811  | 34.3 |
| IV                              | 40804  | 34.2                           | 1.0    | -3425  | -9.9                           | 99.0    | 41258  | 34.2 |

- 1) Note that I = 10 per cent poorest households  
 II = 80 per cent in the middle of the distribution of households' disposable income  
 III = 10 per cent richest households  
 IV = all households

**Table 13. Distribution of equivalent variation by household income<sup>1)</sup> under 1992-taxes.**

**Sweden**

| Equivalent variations, SEK 1992 |  |                                |        |  |                                |         |  |      |
|---------------------------------|--|--------------------------------|--------|--|--------------------------------|---------|--|------|
| Total                           |  |                                | Losers |  |                                | Winners |  |      |
| Mean                            | EV<br>relative to<br>average tax<br>Per cent | Per cent<br>of popu-<br>lation | Mean   | EV<br>Relative to<br>Average tax<br>Per cent | Per cent<br>of popu-<br>lation | Mean    | EV<br>relative to<br>average tax<br>Per cent |      |
| I                               | -8451  | -15.2                          | 95.2   | -9420  | -17.5                          | 4.8     | 10503  | 13.0 |
| II                              | 1960   | 1.8                            | 58.4   | -8350  | -9.6                           | 41.6    | 16433  | 11.3 |
| III                             | 49962  | 20.4                           | 3.6    | -7642  | -7.2                           | 96.4    | 52139  | 20.3 |
| IV                              | 5722   | 4.8                            | 56.6   | -8525  | -10.5                          | 43.4    | 24291  | 14.3 |

- 1) Note that I = 10 per cent poorest households  
 II = 80 per cent in the middle of the distribution of households' disposable income  
 III = 10 per cent richest households  
 IV = all households

#### **4. Summary and discussion**

Tax system competition may change the current progressive tax systems in Europe towards a proportional tax on income. This process may lead to proportional tax rates that differ across country to account for initial differences in tax revenues.

The objective of this paper is to examine the welfare effects for married couples from replacing current tax systems by a proportional labor income tax. To broaden the relevance of our study we compare Norway and Sweden with Italy, which has a low degree of progression in the taxation of labor income by Scandinavian standards. Based on a microeconomic labor supply model estimated on data from the three countries, we have simulated labor supply responses and welfare gains and losses for married couples from replacing the country-specific 1992-tax systems by proportional taxation. The flat tax rates are chosen so as to keep the tax revenues fixed and equal to the country-specific 1992-revenue. The simulation results show that the proportional tax rates vary from 23 (Italy), 25 (Norway) to 29 percent (Sweden) which are close to the current tax rates on capital income. The mean welfare effect from introducing proportional taxation is found to be positive which indicates that there are efficiency costs associated with the current progressive labor income taxes. However, the results reveal large variation in the distribution of welfare gains and losses. Rich households — defined by their pre-reform income — tend to benefit more than the poor. Moreover, the losers tend to have lower pre-tax-reform incomes than the winners.

In the calculation of welfare gains and losses at the household level we have employed the widely used concept of Equivalent Variation (EV). EV is a money measure of the welfare change and may be interpreted as a money measure of the household's willingness to accept the current tax system instead of having an alternative tax system say, a flat tax on income. If EV is positive, then the household considers the alternative tax system to be better than the current one. Although the aggregate of EV across households is a commonly used money measure of welfare change in the total population, (see Rosen(1996) for a recent application), it is also a rather controversial one, and for two reasons. First, it requires a particular cardinalization of households' utility functions that should also be comparable across households. Second, it implies an utilitarian social welfare function where all households are given equal welfare weights. However, in case we do not permit the utility differences to be comparable across households, judgements based on an ordinal representation of preferences nevertheless allow for determining the losers and winners of the reform. In our case a majority in Italy and Sweden lose from having a flat tax on labor income, while in Norway a majority wins. Thus, if

a flat tax rate reform were to be decided in a referendum, our results indicate that it would have received a yes in Norway and a no in Sweden in Italy. However, it should be emphasized that these results depend, *inter alia*, on the demographic and educational structure of the households used in the simulations.

Female labor supply responses are high in Norway and modest in Italy and Sweden. The weak labor supply responses for Italy are due to rigidity of working hours in the opportunity sets and to the fact that the 1992 tax system did not differ much from a proportional tax system, whilst the low responses in Sweden may be due to stricter regulations of working hours and high incomes.

The transition from progressive to proportional taxation reinforces the efficiency gains from a freer trade in Europe caused by the dismantling of borders. Then one may ask whether the reduction in loss of efficiency is attained at the cost of increased income and welfare inequality. Our results, however, do not indicate any sharp increase in income inequality. On the contrary, in the case of Norway we find that the inequality in the distribution of gross household income is reduced to an extent that the distribution of the net household income is even made more equal. However, when the value of leisure is taken into account, we find that the welfare of rich households, measured by EV, — in particular in Norway — increases far more than the welfare of poor households.

## Appendix 1. Empirical specifications and estimation results

### Norway

Let the subscript  $F$  and  $M$  denote female and male, respectively. In the case of married couples the structural part of the utility function defined by (6) is

$$\begin{aligned} \log v(C, h_F, h_M) = & \mathbf{a}_2 \left( \frac{(10^{-4} C)^{\mathbf{a}_1} - 1}{\mathbf{a}_1} \right) + \left( \frac{L_M^{\mathbf{a}_3} - 1}{\mathbf{a}_3} \right) (\mathbf{a}_4 + \mathbf{a}_5 \log A_M + \mathbf{a}_6 (\log A_M)^2) \\ & + \left( \frac{L_F^{\mathbf{a}_7} - 1}{\mathbf{a}_7} \right) (\mathbf{a}_8 + \mathbf{a}_9 \log A_F + \mathbf{a}_{10} (\log A_F)^2 + \mathbf{a}_{11} CU6 + \mathbf{a}_{12} CO6) + \mathbf{a}_{13} L_F L_M \end{aligned} \quad (\text{A.1})$$

where  $A_F, A_M$  are the age of the wife and the husband, respectively,  $CU6$  and  $CO6$  are number of children less than 6 and above 6 years,  $L_K$  is leisure for gender  $k = M, F$ , defined as

$$L_K = 1 - h_K / 8760, \quad (\text{A.2})$$

and  $\mathbf{a}_j, j=1,2,\dots,13$ , are unknown parameters.

$$\text{If } \mathbf{a}_1 < 1, \mathbf{a}_3 < 1, \mathbf{a}_7 < 1, \mathbf{a}_2 > 0,$$

$$\mathbf{a}_4 + \mathbf{a}_5 \log A_M + \mathbf{a}_6 (\log A_M)^2 > 0,$$

and

$$\mathbf{a}_8 + \mathbf{a}_9 \log A_F + \mathbf{a}_{10} (\log A_F)^2 + \mathbf{a}_{11} CU6 + \mathbf{a}_{12} CO6 > 0$$

then  $\log v(C, h_F, h_M)$  is increasing in  $C$ , decreasing in  $(h_F, h_M)$  and strictly concave in  $(C, h_F, h_M)$ .

It is assumed that the offered hours is not correlated with offered wage rates, which may be justified by the fact that in most countries working hours are regulated by law or set in central negotiations between unions and employers associations. The fraction of jobs with a given number of hours is assumed to be consistent with a uniform distribution of hours apart from a peak at full-time hours for males and part-time hours for females. The fraction of jobs with a given wage rate is assumed to be a log normal density with gender-specific means that depend on length of schooling and on experience. "Experience" is defined as age minus length of schooling minus six.

The results from estimating the model on Norwegian data from 1986 are given in Table 14.

Note that most parameters are rather precisely determined and have the theoretically expected signs.

The estimates are in accordance with the theory in the sense the mean utility function is an increasing and strictly concave function in consumption and leisure. The males marginal mean utility of leisure in Norway attains a minimum at the age of 41.9 years and in the case of females, at the age of 35 years. The wife's education turns out to affect the fraction of feasible job opportunities such that a higher educated woman has more job opportunities than a less educated one. (Implied by  $\hat{\alpha}_{15} < 0$ .)

For the estimate of the wage opportunity density we refer to Aaberge et al. (1995).

**Table 14. Estimates of the parameters of the utility function and of the opportunity density. Norway 1986**

| Variables                  | Coefficient   | Estimates | t-values |
|----------------------------|---------------|-----------|----------|
| <u>Preferences:</u>        |               |           |          |
| Consumption                | $\alpha_1$    | 0.951     | 16.4     |
|                            | $\alpha_2$    | 1.269     | 5.6      |
| Male leisure               | $\alpha_3$    | -4.312    | 6.8      |
|                            | $\alpha_4$    | 100.598   | 3.0      |
|                            | $\alpha_5$    | -53.091   | 3.0      |
|                            | $\alpha_6$    | 7.270     | 3.0      |
| Female leisure             | $\alpha_7$    | -2.240    | 5.5      |
|                            | $\alpha_8$    | 237.438   | 3.9      |
|                            | $\alpha_9$    | -130.174  | 3.9      |
|                            | $\alpha_{10}$ | 18.492    | 4.1      |
|                            | $\alpha_{11}$ | 3.397     | 6.4      |
|                            | $\alpha_{12}$ | 1.648     | 4.8      |
| Leisure interaction term   | $\alpha_{13}$ | 0         |          |
| <u>Opportunities:</u>      |               |           |          |
| Female opportunity measure | $\alpha_{14}$ | 0.063     | 0.1      |
|                            | $\alpha_{15}$ | -0.203    | 3.7      |
| Male opportunity measure   | $\alpha_{16}$ | -3.296    | 4.5      |
| Interaction                | $\alpha_{17}$ | 1.289     | 4.5      |
| Full-time peak, males      | $\alpha_{18}$ | 1.062     | 11.2     |
| Full-time peak, females    | $\alpha_{19}$ | 0.710     | 5.8      |
| Part-time peak, females    | $\alpha_{20}$ | 0.425     | 2.5      |

## Sweden

The structural part of the utility function is defined by

$$\begin{aligned}
 \log v(C, h_F, h_M) = & \mathbf{a}_2 \left( \frac{(10^{-5} C - 0.3)^{\mathbf{a}_1} - 1}{\mathbf{a}_1} \right) + \left( \frac{L_M^{\mathbf{a}_3} - 1}{\mathbf{a}_3} \right) (\mathbf{a}_4 + \mathbf{a}_5 \log A_M + \mathbf{a}_6 (\log A_M)^2) \\
 & + \left( \frac{L_F^{\mathbf{a}_7} - 1}{\mathbf{a}_7} \right) (\mathbf{a}_8 + \mathbf{a}_9 \log A_F + \mathbf{a}_{10} (\log A_F)^2 + \mathbf{a}_{11} CU6 + \mathbf{a}_{12} CO6) \\
 & + \mathbf{a}_{13} L_F^{0.5\mathbf{a}_3} L_M^{0.5\mathbf{a}_7}
 \end{aligned} \tag{A.3}$$

The fraction of jobs with a given number of hours is assumed to be consistent with a uniform distribution of hours apart from a peak at full-time hours for males and peaks at full-time, 2/3 part-time and part-time hours for females. The reason why there are more peaks in the Swedish female case than in the corresponding Norwegian case is that there are more strict regulation of part-time working hours in the Swedish labor market than in the Norwegian.

The Swedish dataset does not allow for the modeling of participation and is thus based on observations for married couples who are working. On the other hand the labor force rates both for males and females are very high in Sweden (highest in the world).

In Table 15 we present the estimates of the Swedish utility function based on household data from 1981.

**Table 15. Estimates of the parameters of the utility function and of the opportunity density, Sweden 1981**

| Variables                   | Coefficient   | Estimates | t-values |
|-----------------------------|---------------|-----------|----------|
| <u>Preferences:</u>         |               |           |          |
| Consumption                 | $\alpha_1$    | 0.574     | 9.4      |
|                             | $\alpha_2$    | 9.278     | 11.4     |
| Male leisure                | $\alpha_3$    | -4.607    | 5.8      |
|                             | $\alpha_4$    | 174.644   | 3.0      |
|                             | $\alpha_5$    | -91.188   | 3.0      |
|                             | $\alpha_6$    | 12.371    | 3.1      |
| Female leisure              | $\alpha_7$    | -4.106    | 6.5      |
|                             | $\alpha_8$    | 153.041   | 2.5      |
|                             | $\alpha_9$    | -78.834   | 2.4      |
|                             | $\alpha_{10}$ | 10.876    | 2.5      |
|                             | $\alpha_{11}$ | 1.541     | 3.8      |
|                             | $\alpha_{12}$ | 0.805     | 3.1      |
| Leisure interaction term    | $\alpha_{13}$ | 1.698     | 1.5      |
| <u>Opportunities:</u>       |               |           |          |
| Full-time peak, males       | $\alpha_{14}$ | 3.424     | 47.1     |
| Full-time peak, females     | $\alpha_{15}$ | 2.814     | 29.1     |
| 2/3 part-time peak, females | $\alpha_{16}$ | 1.454     | 13.5     |
| Part-time peak, females     | $\alpha_{17}$ | 1.830     | 18.8     |

Note that most parameters are rather precisely determined (apart from the cross leisure term) and they have the theoretically expected signs.

The estimates imply that the mean utility function is an increasing and strictly concave function in consumption and leisure. The males marginal mean utility of leisure attains a minimum at the age of 41.9 years and in the case of females, at the age of 35 years, exactly the same as for Norway.

The estimated wage opportunity density and aggregate labor supply elasticities are reported in Aaberge et al. (1990).



## Italy

The functional form of the deterministic part of the utility function is defined by

$$\begin{aligned} \log v(C, h_F, h_M) = & \left[ \mathbf{a}_2 (1 - K_M)(1 - K_F) + \mathbf{a}_3 K_F + \mathbf{a}_4 K_M \right] e^{\mathbf{a}_1 C} \\ & + \left[ \mathbf{a}_6 + \mathbf{a}_7 \log A_M + \mathbf{a}_8 (\log A_M)^2 \right] \left( \frac{L_M^{\mathbf{a}_5} - 1}{\mathbf{a}_5} \right) \\ & + \left[ \mathbf{a}_{10} + \mathbf{a}_{11} \log A_F + \mathbf{a}_{12} (\log A_F)^2 + \mathbf{a}_{13} CU6 + \mathbf{a}_{14} CO6 \right] \left( \frac{L_F^{\mathbf{a}_9} - 1}{\mathbf{a}_9} \right) \end{aligned} \quad (\text{A.4})$$

$K_j = 1$  if spouse  $j$  is working; otherwise  $K_j = 0$ , and the specification implies that the marginal utility of consumption differs with respect to the reported labor market participation. The reason for doing this is the possible existence of non-reported income. The underground economy in Italy is believed to be of some importance. To capture some of these effects on income and hence on consumption, the marginal utility of consumption is specified as (implicitly) shown above.

Since the regional variation of wages is more important than in the Scandinavian countries, and since unemployment in Italy has been rather high by Norwegian/Swedish standards, we will include a discussion of the estimation of the wage opportunity density here. The opportunity measure for wages are specified as follows,

$$\log W_j(z) = \mathbf{b}_{0j} + \mathbf{b}_{1j} s_j + \mathbf{b}_{2j} \text{Exp}_j + \mathbf{b}_{3j} (\text{Exp}_j)^2 + \mathbf{b}_{4j} \text{Re } g_j + \mathbf{h}_j(z) \quad (\text{A.5})$$

$j = F, M$ , where  $(\mathbf{h}_F(z), \mathbf{h}_M(z))$  are normally distributed,  $s_j$  denotes years of schooling, gender  $j$ ,  $\text{Exp}_j = \text{experience} = A_j - s_j - 6$  and  $\text{Re } g = 1$  living in Northern Regions (North of Tuscany) and 0 otherwise. Moreover,

$$\log(g_{01}) = \mathbf{a}_{15} + \mathbf{a}_{16} \text{Re } g_F + \mathbf{a}_{17} UE_F, \quad (\text{A.6})$$

and

$$\log(g_{10}) = \mathbf{a}_{18} + \mathbf{a}_{19} \text{Re } g_M + \mathbf{a}_{20} UE_M \quad (\text{A.7})$$

where  $UE_j$  is the ratio between the number of unemployed and employed for gender  $j$ .

It should be noted that the specifications (A.6) and (A.7) imply the following interpretation of the model parameters. If  $\mathbf{a}_{16}$  and  $\mathbf{a}_{19}$  are positive, then living in Northern Italy improves the chances of finding a market opportunity, compared to living in Central and Southern Italy. Likewise,

negative values of  $\alpha_{17}$  and  $\alpha_{20}$  indicate that unemployment has a negative impact on job opportunities.

Feasible hours in the market is assumed to be uniformly distributed except for peaks at full-time hours for females and males, which are defined by the interval [1846, 2106]. Note that this interval corresponds to weekly hours between 36 and 40.

The estimation results are reported in Table 16.

**Table 16. Estimates of the parameters of the utility function and of the opportunity density, Italy 1987.**

| Variables                  | Coefficient   | Estimates              | t-values |
|----------------------------|---------------|------------------------|----------|
| Consumption                | $\alpha_1$    | $-0.780 \cdot 10^{-4}$ | -7.7     |
|                            | $\alpha_2$    | -15.938                | -8.3     |
|                            | $\alpha_3$    | -10.020                | -19.1    |
|                            | $\alpha_4$    | -15.364                | -11.4    |
| Male leisure               | $\alpha_5$    | -18.651                | -16.4    |
|                            | $\alpha_6$    | -0.180                 | -1.4     |
|                            | $\alpha_7$    | 0.102                  | 1.5      |
|                            | $\alpha_8$    | -0.015                 | -1.4     |
| Female leisure             | $\alpha_9$    | -6.805                 | -8.1     |
|                            | $\alpha_{10}$ | 34.428                 | 2.2      |
|                            | $\alpha_{11}$ | -19.039                | -2.2     |
|                            | $\alpha_{12}$ | 2.716                  | 2.3      |
|                            | $\alpha_{13}$ | 0.225                  | 1.8      |
|                            | $\alpha_{14}$ | 0.275                  | 2.7      |
| Female opportunity density | $\alpha_{15}$ | -0.952                 | -2.8     |
|                            | $\alpha_{16}$ | 0.705                  | 6.5      |
|                            | $\alpha_{17}$ | -0.594                 | -0.9     |
| Male opportunity density   | $\alpha_{18}$ | -0.512                 | -8.4     |
|                            | $\alpha_{19}$ | 0.310                  | 1.2      |
|                            | $\alpha_{20}$ | 0.243                  | 0.1      |
| Full-time peak, males      | $\alpha_{21}$ | 2.406                  | 28.0     |
| Full-time peak, females    | $\alpha_{22}$ | 2.501                  | 51.9     |

The estimates imply that the deterministic part of the utility function is an increasing and strictly concave function of leisure and consumption. The basic parameters of the utility function are

$a_1$ ,  $a_5$  and  $a_9$ . These parameters are measured with good precision. The marginal utility of consumption and leisure depends also on personal characteristics such as age and number of children. The estimates for the coefficients of these variables are less precise. Children have the expected positive effect on the value of wife's leisure. However, a rather surprising result is that the presence of older children have essentially the same effect as younger ones; as a matter of fact the point estimate for the former ones is even larger (this result, however, accords with other analyses of Italian data, see e.g. Colombino and Del Boca (1990)). A possible explanation might be found in a cohort effect. Women with older children on average belong to older cohorts. For a variety of unobserved factors (attitudes, supply of child-care services, etc.) which change from one cohort to the other, older cohorts presumably tend to use a more "leisure-intensive" technology in child-care.

The estimated parameters of the job-opportunities density confirm – at least for females – a more favourable environment in Northern regions. On the other hand, the effect of unemployment is not measured precisely enough to draw any clear conclusion. For a more comprehensive discussion of the empirical results we refer to Aaberge et al. (1993) who also report the estimated wage opportunity density and various aggregate labor supply elasticities.

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